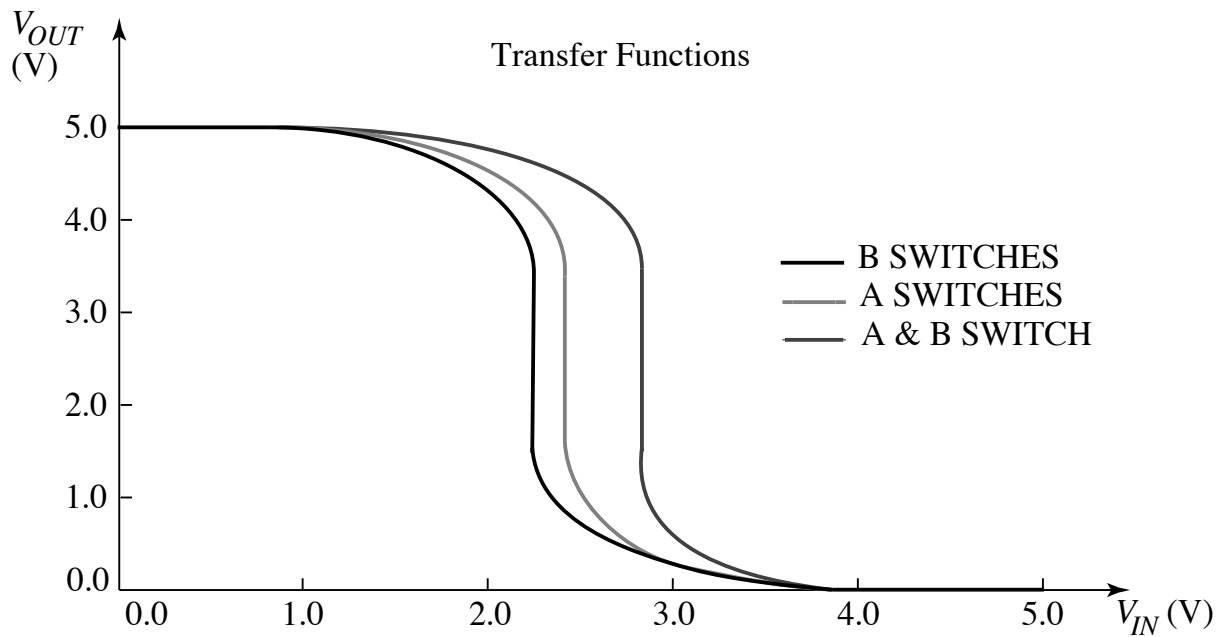


NAND Gate Transfer Functions

- SPICE is useful to solve for the transfer functions under the various switching conditions (see Ex. 5.7). Note that the backgate effect means that the curves when V_A switches and when V_B switches are not identical.



- Results: setting $k_n = 2 k_p$ results in V_M approximately $V_{DD}/2$.

CMOS NAND Gate Transient Analysis

- Worst-case situation for low-to-high transition: only one of the p-channel transistors is switching (say M_4):

$$-I_{Dp} = -I_{D4} = \frac{k_p}{2}(V_{DD} + V_{Tp})^2$$

- For high-to-low transition, consider M_1 and M_2 in series with effective length at $2L_n$ (worst-case since current is lowest with $V_A = V_B$)

$$I_{Dn} = I_{D1} = I_{D2} = \mu_n C_{ox} [W_n / 2(2L_n)] (V_{DD} - V_{Tn})^2 = \frac{k_n}{4} (V_{DD} - V_{Tn})^2$$

- For equal propagation delays, we require $I_{Dn} = -I_{Dp}$

$$\frac{k_n}{4} = \frac{k_p}{2} \rightarrow k_n = 2k_p$$

The factor of 2 mobility difference between the p and n channels indicates that

$$(W/L)_n = (W/L)_p \text{ (2 input NAND gate)}$$

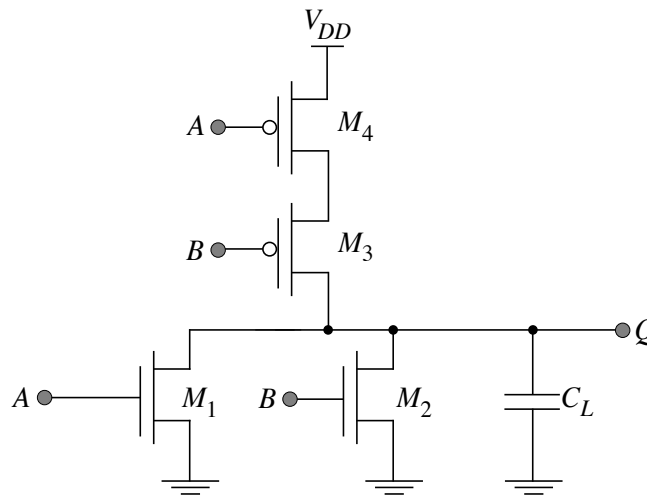
- For an M -input NAND gate, we find that

$$(W/L)_n = (M/2) (W/L)_p$$

Note: NOR gates suffer from a factor of $2M$ between the n- and p-channel ratios which makes them unattractive for large fan-in gates

CMOS Dynamic Logic

- Static NOR gate



Idea: n-channel and p-channel devices separately perform the same logic function.

replace p-channels with a resistor -->

$$Q = \overline{A + B}$$

replace n-channels with a resistor -->

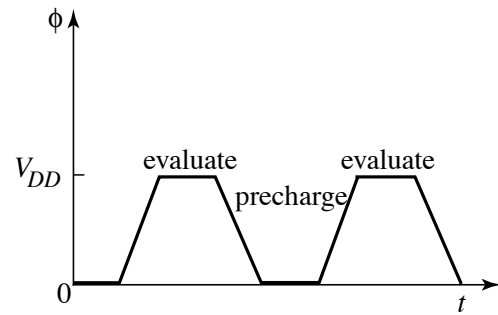
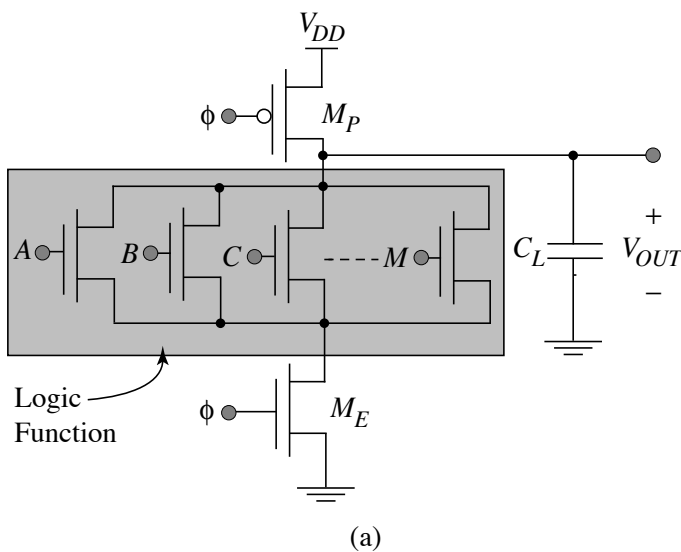
$$Q = \overline{\overline{A}\overline{B}}$$

... two functions are identical by DeMorgan's Theorem

- Let n-channels perform the logic and get rid of the pull-up devices (or vice versa)

n-Channel CMOS Dynamic Logic

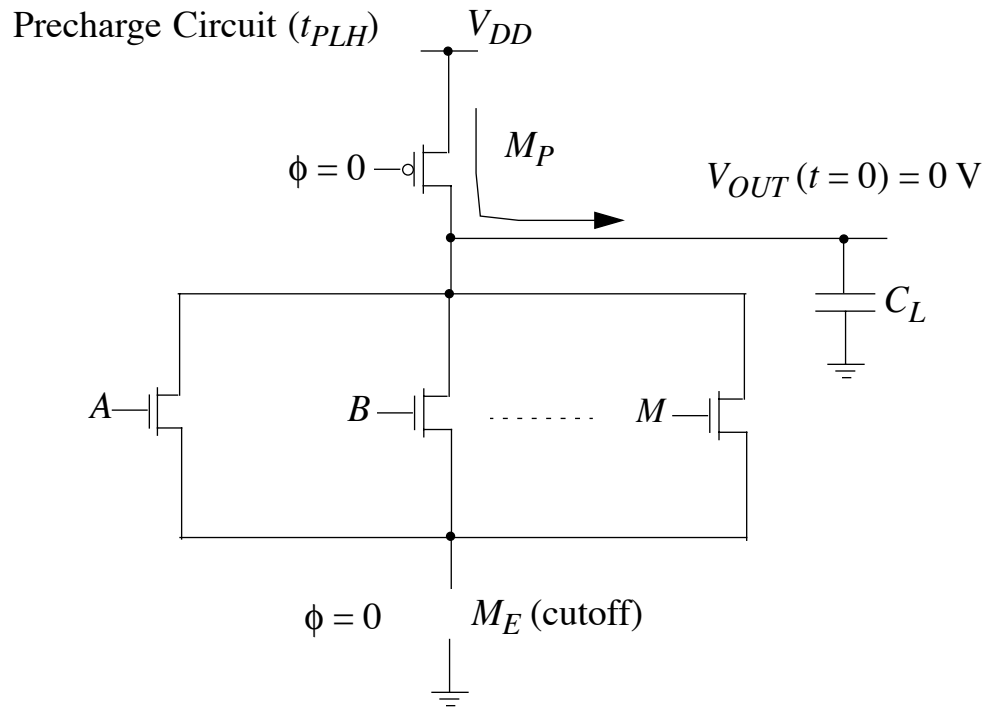
- clock signal $\phi(t)$ charges up load capacitance through M_P ($P = \text{precharge}$) when it transitions from high to low; M_E ($E = \text{evaluate}$) is cutoff and prevents any discharge path of C_L through logic function transistors.
- clock signal goes high $\rightarrow M_P$ is cutoff, M_E conducts $\rightarrow C_L$ discharges if one of the logic transistors has a high input.



- Payoffs:
 1. large fan-in NOR gates without huge p-channel load devices (also, avoids backgate effect on loads)
 2. tends to be fast due to smaller load capacitances
- Drawback:
 1. clock is essential to refresh logic level stored on C_L , which complicates the design

n-Channel Dynamic Logic Propagation Delays

- Consider “ t_{PLH} ” to be the time required to pre-charge the output node



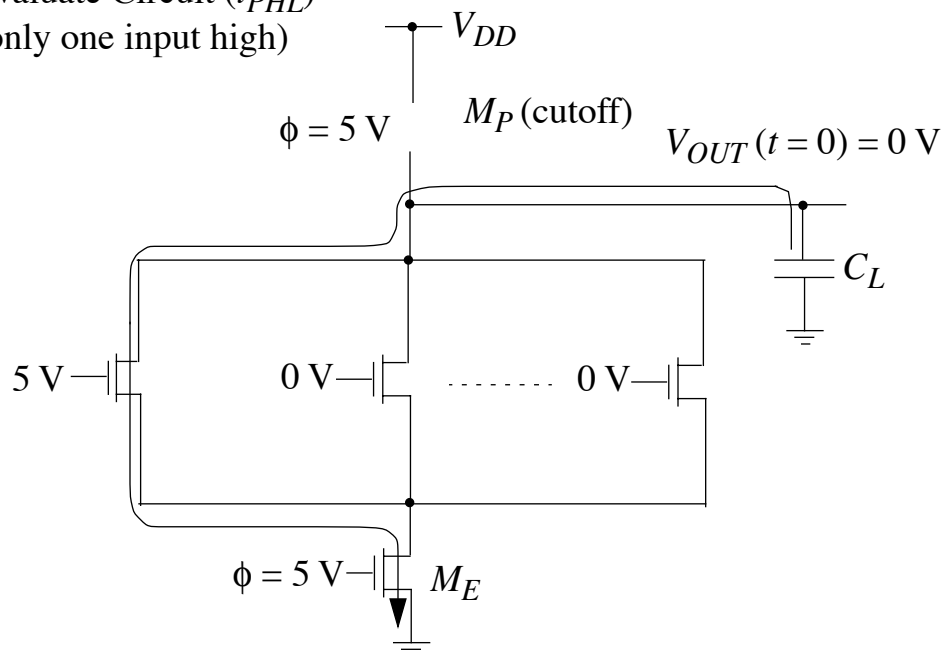
- Charging current

$$-I_{Dp} = \frac{k_p}{2}(V_{DD} + V_{Tp})^2$$

n-Channel Dynamic Logic Propagation Delays

- Consider “ t_{PHL} ” to be the *worst-case* time to evaluate the logical function after clock goes high.

Evaluate Circuit (t_{PHL})
(only one input high)

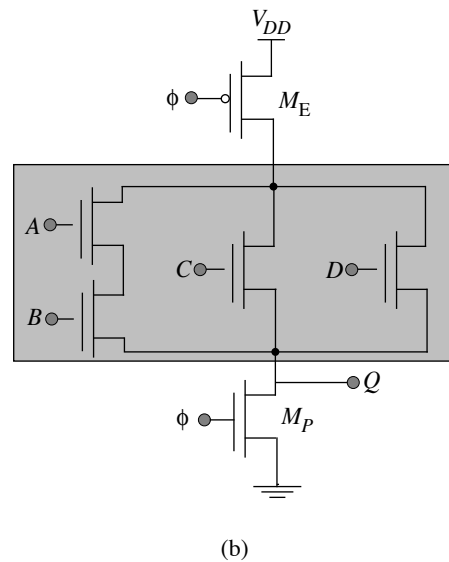
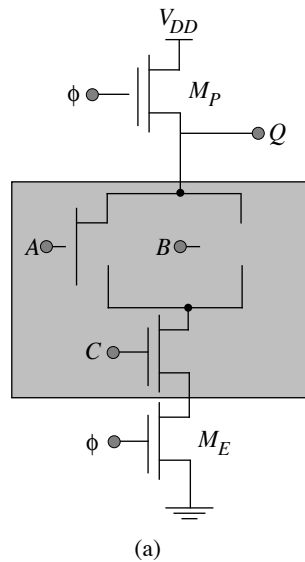


- Discharging current: assume $(W/L)_E = (W/L)_A = \dots (W/L)_M$ and note that the transistors are in series --> effective value is $k_n / 2$

$$I_{D_n} = \mu_n C_{ox} \left(\frac{k_n}{4} \right) (V_{DD} - V_{Tn})^2$$

Boolean Functions in Dynamic Logic

- Examples:



- (a) n-channel dynamic logic

$$Q = \overline{(A + B)C}$$

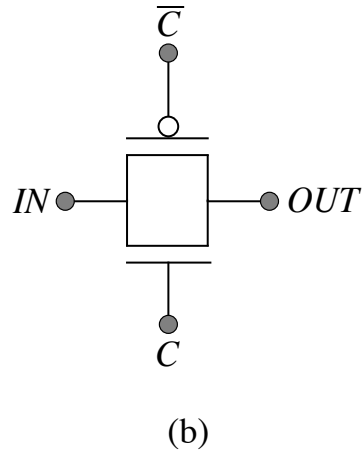
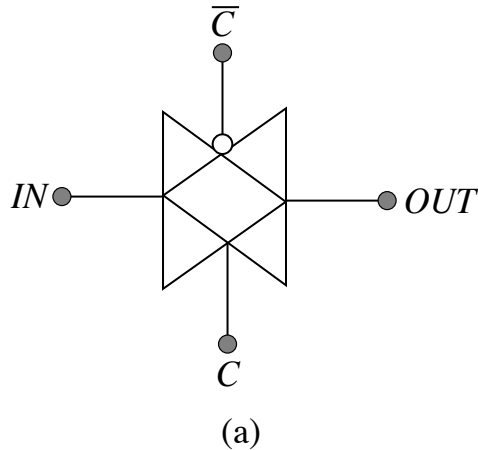
- (b) p-channel dynamic logic

The output is “pre-discharged” to zero by M_P and is only charged if there is a path through the logic transistors when the clock goes low and M_E conducts.

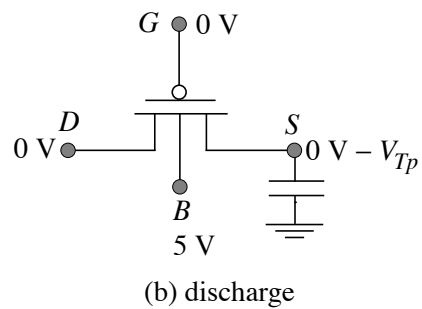
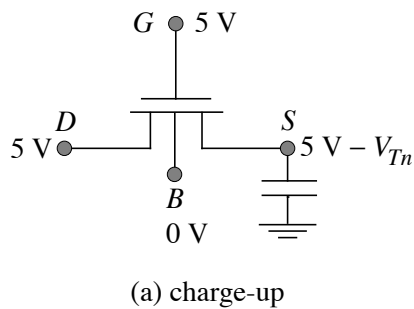
$$Q = \bar{A}\bar{B} + \bar{C} + \bar{D}$$

CMOS Transmission Gates

- Need: “gate” signals by having a series switch that can be shorted or open-circuited.



- Why n-channel and p-channel in parallel? Only one device (say, n-channel): can't pass an input voltage $> V_{DD} - V_{Tn}$, since device will enter the cutoff region



Pass Transistor Logic

- Advantages: reduced transistor count and higher speed compared with static CMOS
- Disadvantage: reduced noise margins

